

9.5.2 The resolution inference rule

The resolution rule for first-order clauses is simply a lifted version of the propositional resolution rule given on page 244. Two clauses, which are assumed to be standardized apart so that they share no variables, can be resolved if they contain complementary literals. Propositional literals are complementary if one is the negation of the other; first-order literals are complementary if one *unifies with* the negation of the other. Thus, we have

$$\frac{\ell_1 \vee \cdots \vee \ell_k, \quad m_1 \vee \cdots \vee m_n}{\text{SUBST}(\theta, \ell_1 \vee \cdots \vee \ell_{i-1} \vee \ell_{i+1} \vee \cdots \vee \ell_k \vee m_1 \vee \cdots \vee m_{j-1} \vee m_{j+1} \vee \cdots \vee m_n)}$$

where $\text{UNIFY}(\ell_i, \neg m_j) = \theta$. For example, we can resolve the two clauses

$$[\textit{Animal}(F(x)) \vee \textit{Loves}(G(x), x)] \quad \text{and} \quad [\neg \textit{Loves}(u, v) \vee \neg \textit{Kills}(u, v)]$$

by eliminating the complementary literals $\textit{Loves}(G(x), x)$ and $\neg \textit{Loves}(u, v)$, with the unifier $\theta = \{u/G(x), v/x\}$, to produce the **resolvent** clause

$$[\textit{Animal}(F(x)) \vee \neg \textit{Kills}(G(x), x)].$$